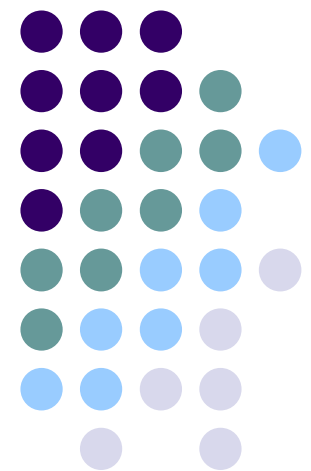
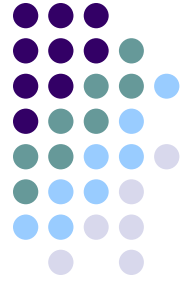


# Process Modeling of Susceptor Assisted Microwave Heating

Shawn Allan, William Keith, Dr. Holly Shulman  
Ceralink Inc.

40<sup>th</sup> Symposium of the  
International Microwave Power Institute  
August 11, 2006

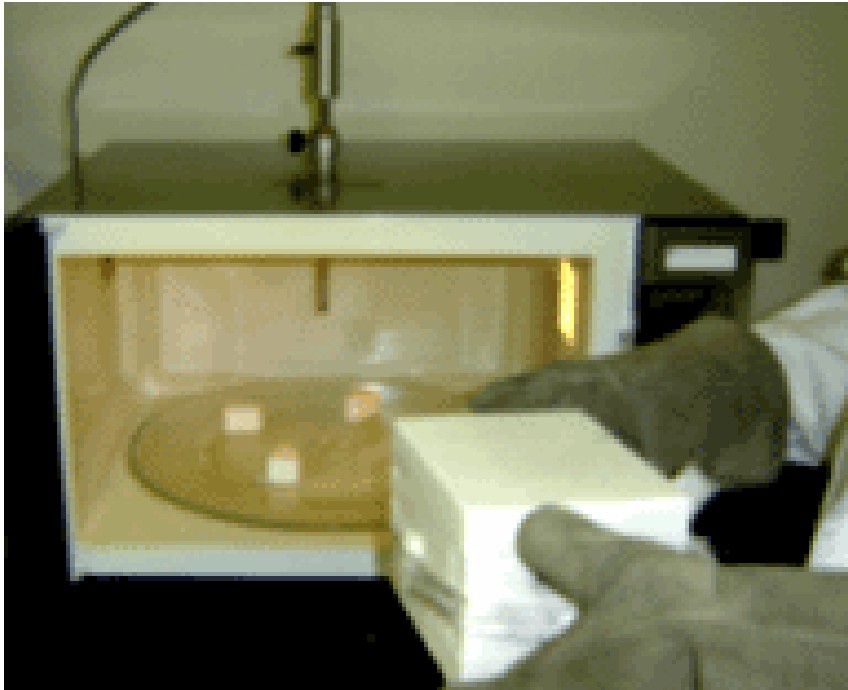
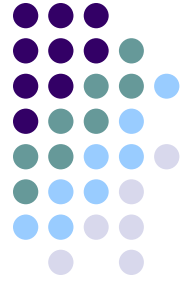




# Outline

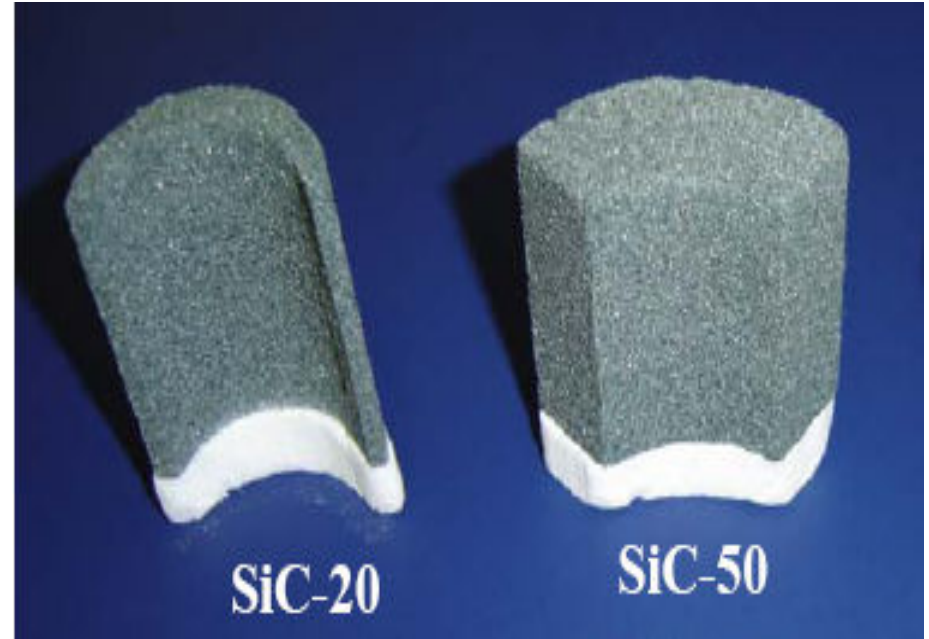
- I. MW susceptors for materials processing
- II. Variables and outputs of susceptor heating
- III. Variable effects on microwave heating
- IV. Calculation of heating profile models
- V. Testing of model
- VI. Conclusions

# I. RMS ThermWave and Thermcept Susceptors



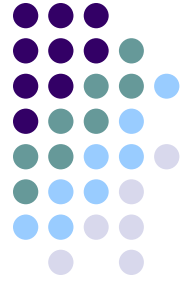
RMS ThermWave  
1.3 kW, 2.45 GHz, water cooled

RMS Thermal Package  
Zircar Ceramics Al-25/1700°C refractory  
Standard sizes



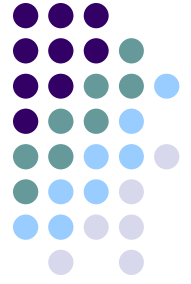
RMS Thermcepts  
SiC-25 – 25 g  
SiC-50 – 50 g





# I. High Temperature Susceptors

- **Susceptors + Microwave Energy**
  - Microwave: volumetric heating (coupling)
  - Susceptor: radiant heating
  - Fast, reliable method for high temperature heating
- **Susceptors couple well at RT**
  - Provide initial heat transfer
  - Minimize temperature gradients
    - Inverse temperature profile
    - Thermal stress failure
- **Limited by power, heat loss, dielectric response**
- **Practical models for microwave users**

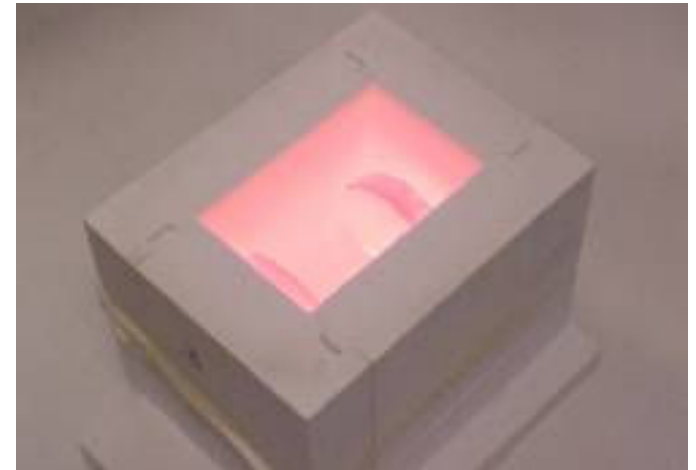


## II. Model Components

- **Variables**

- Susceptor mass
- Thermal package volume
- Power input
- Time

**m**  
**V**  
**P**  
**t**



- **Outputs**

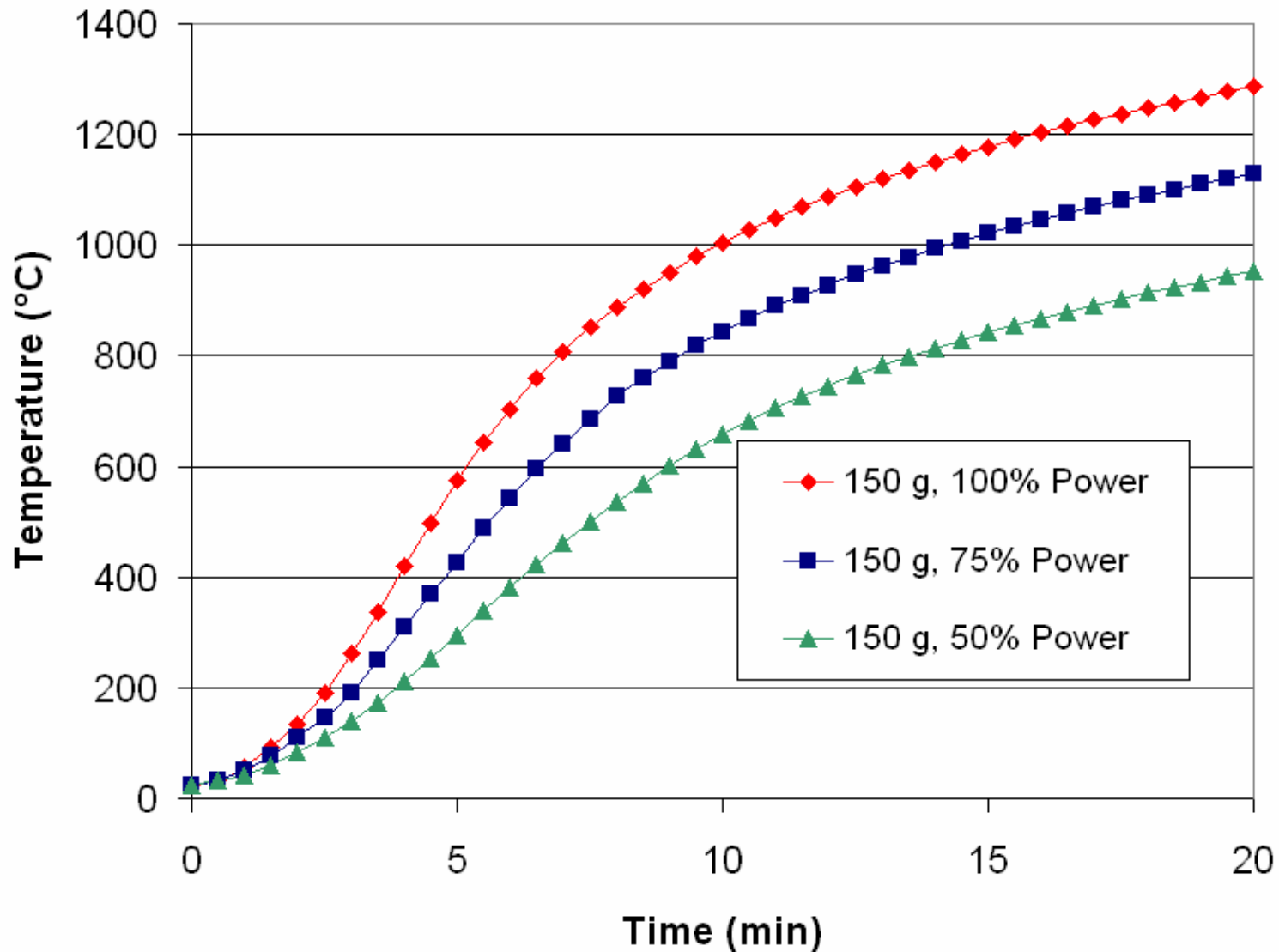
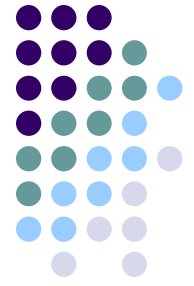
- Temperature (T)
- Heating Rate ( $\partial T/\partial t$ )
- Energy Consumption (E)

$$T = f(m, V, P, t)$$

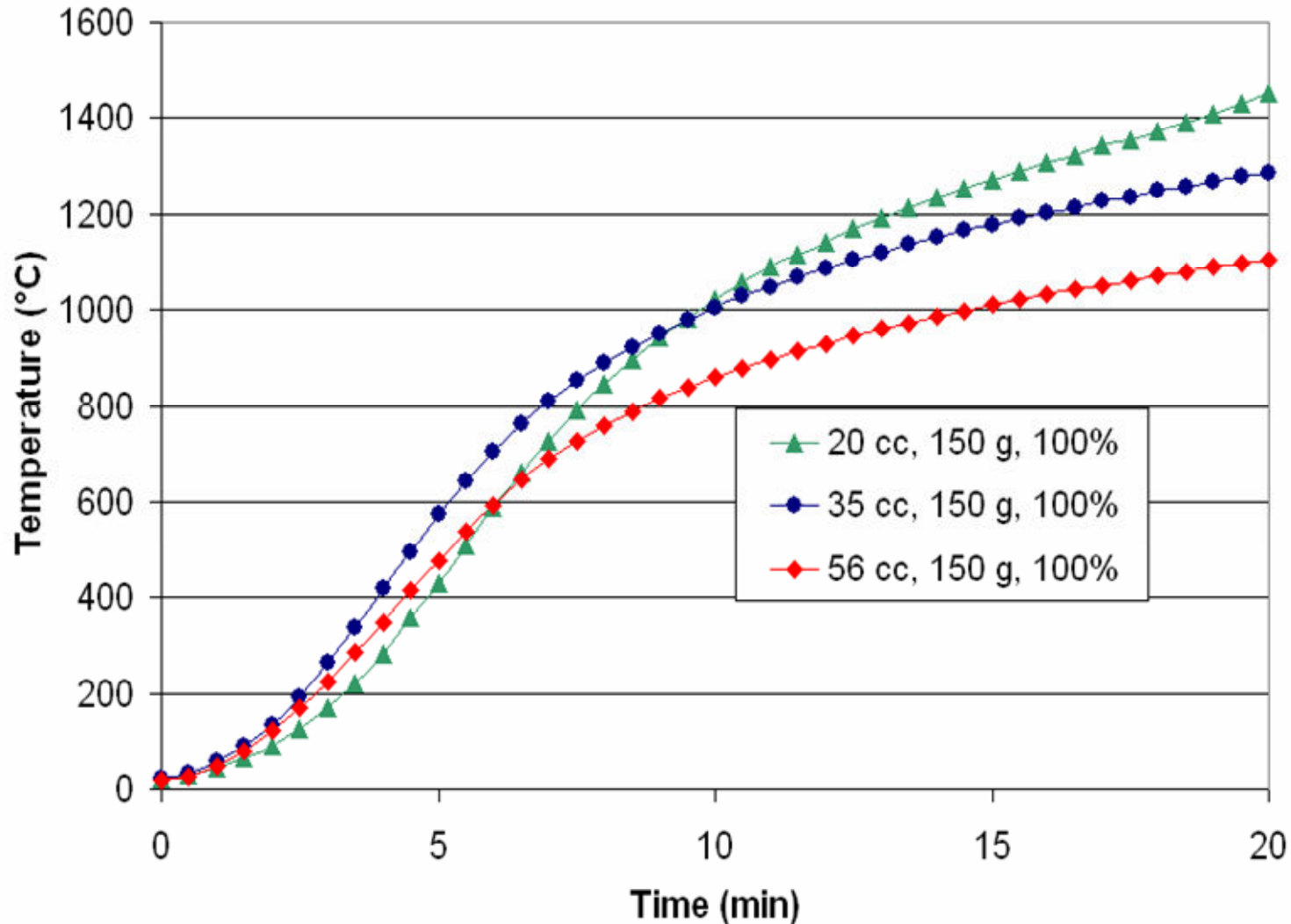
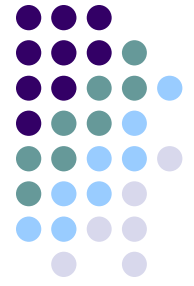
$$(\partial T/\partial t) = g(m, V, P, t)$$

$$E = h(P, t)$$

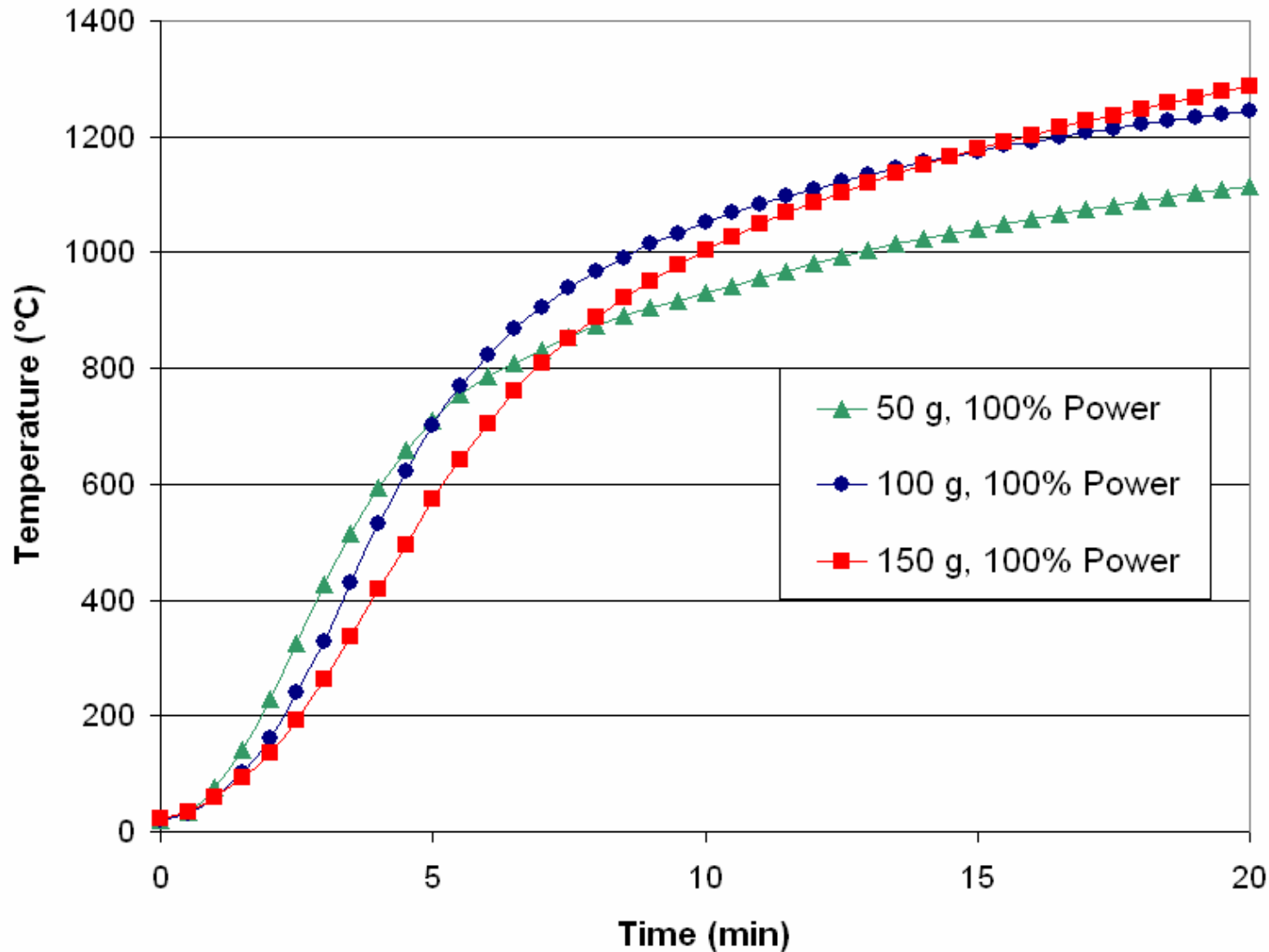
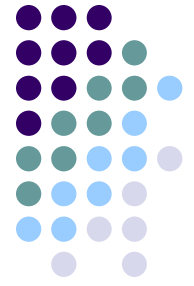
# III. Power Effect – Constant Mass, Volume

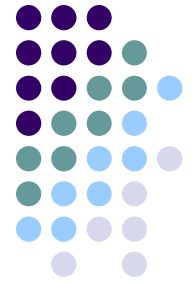


# III. Volume Effect – Constant Mass, Power

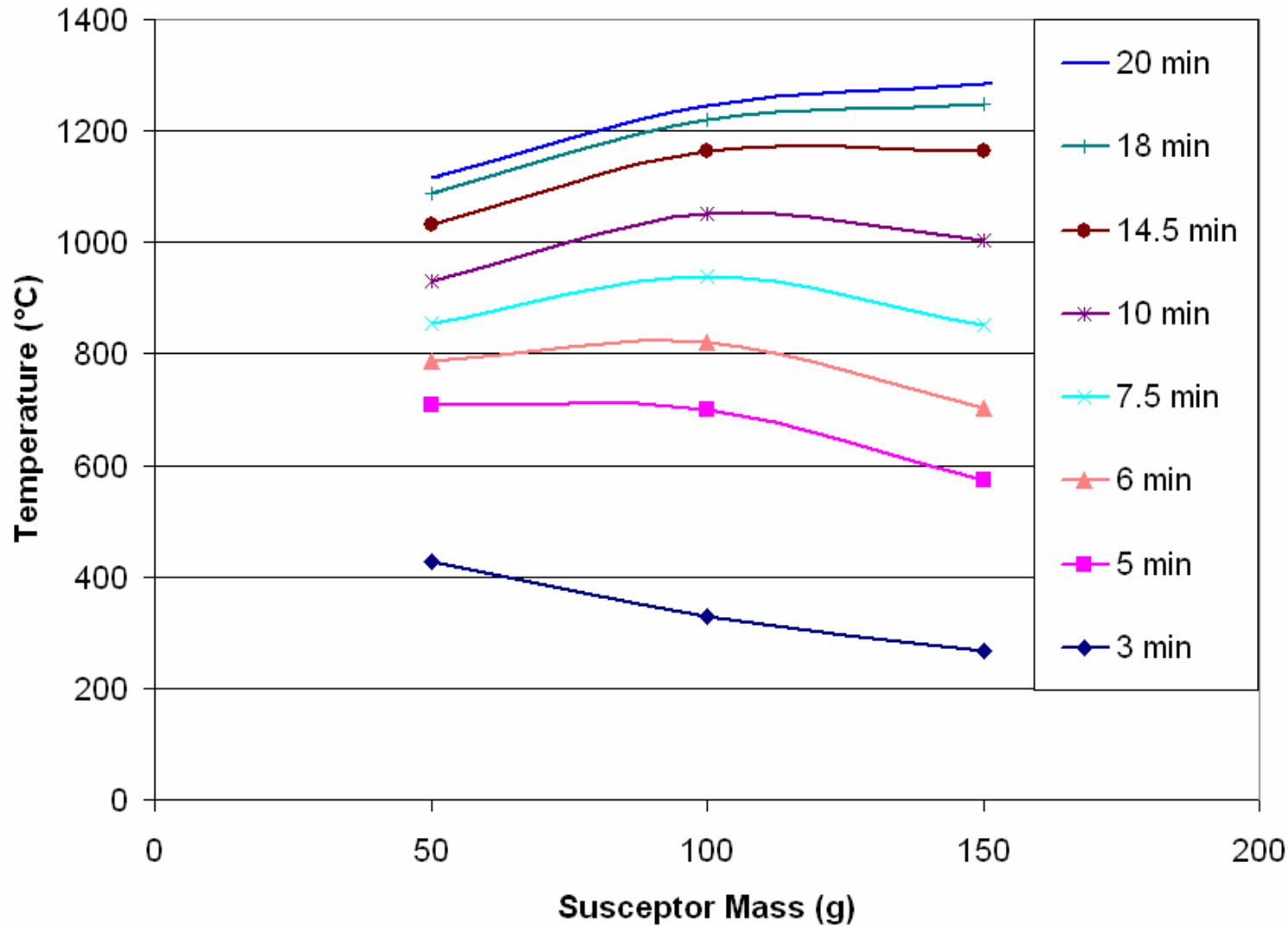


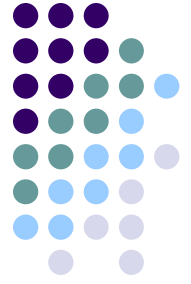
# III. Mass Effect – Constant Power, Volume





# III. Mass and Time Interactions





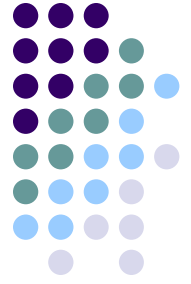
## IV. Curve Fitting $T = F(m, V, P, t)$

- Polynomial fitting

$$T = a + bx_1 + cx_2 + dx_3 \dots nx_k$$

- Sigmoidal fitting (S-curve)

$$F(t) = c1 + \frac{(c2 - c1)}{\left(1 + \left(\frac{t}{c3}\right)^{c4}\right)}$$



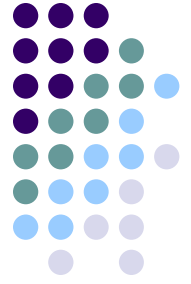
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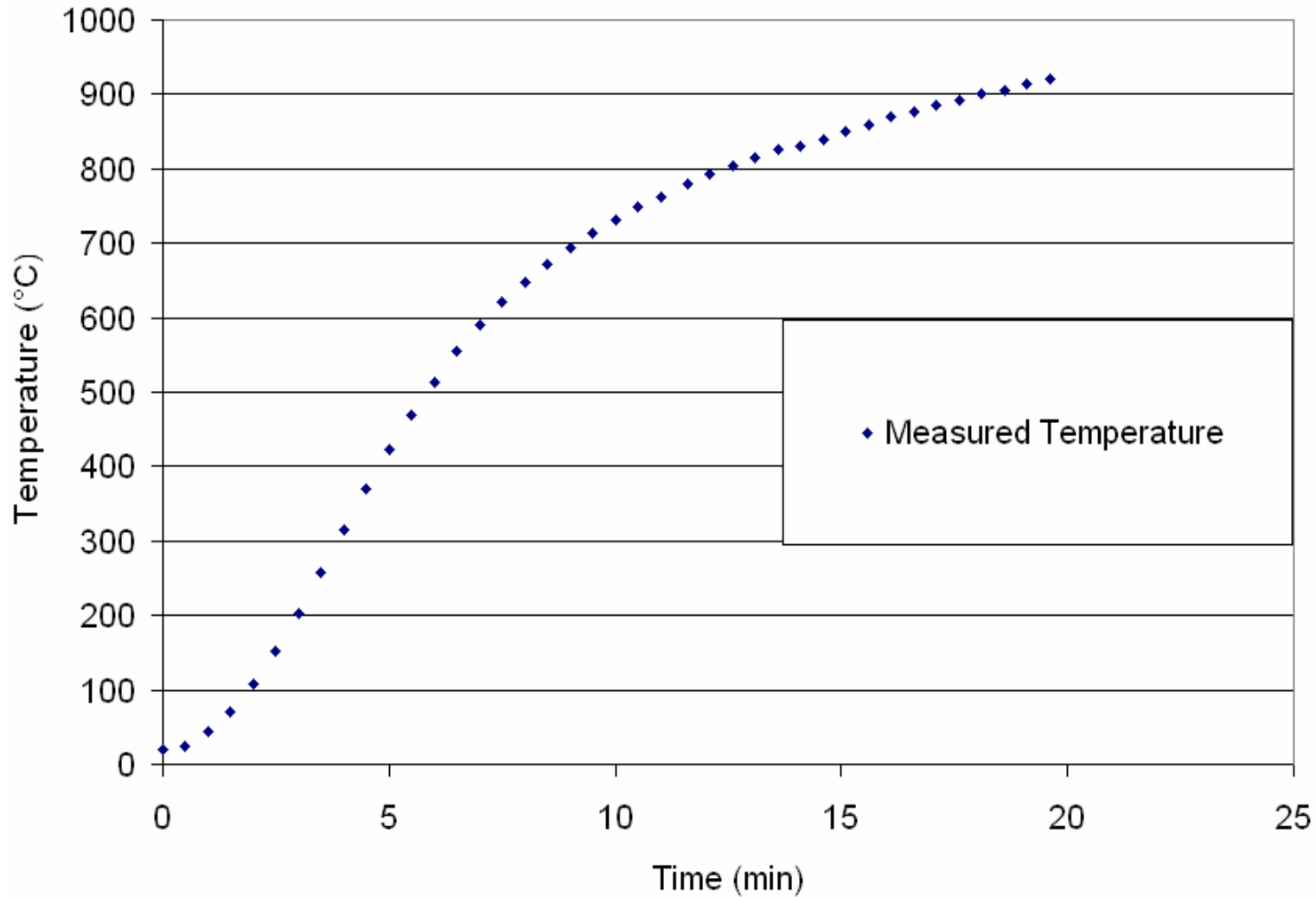
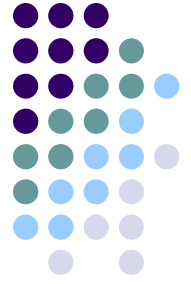


## IV. Sigmoidal Fitting

- Heating curve has S-shape
- Heating limited by microwave power
- Energy In = Energy Out  $\rightarrow$  T plateau
- When  $t=0$ ,  $F(t) = c_2$ ,  $\therefore c_2 = T_0$
- Linear regression for each T-t profile
  - $c_1 = F(m, V, P)$   $R^2 = 0.983$
  - $c_3 = G(m, V, P)$   $R^2 = 0.948$
  - $c_4 = H(m, V, P)$   $R^2 = 0.543$

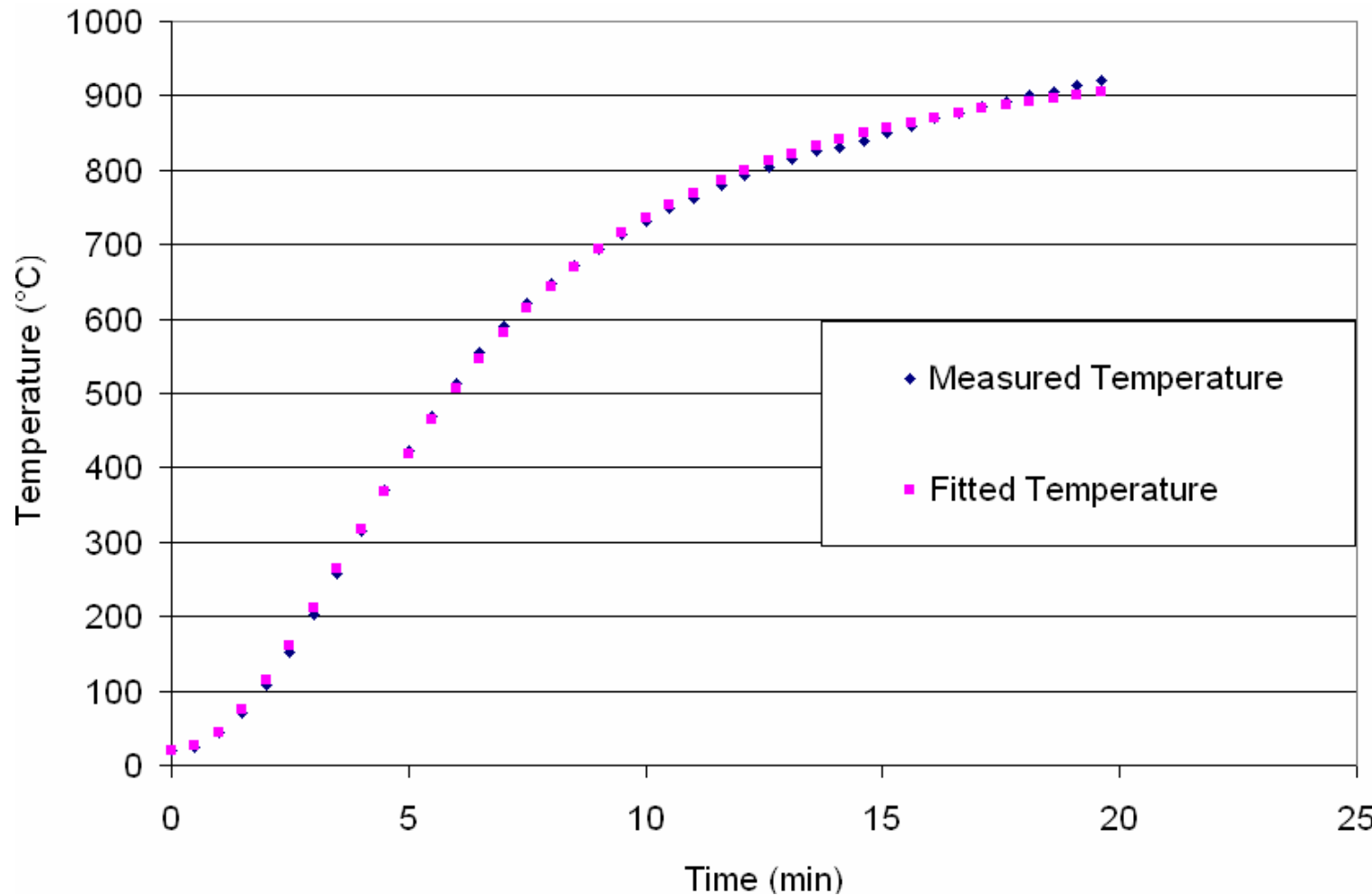
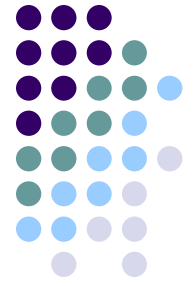
# IV. Sigmoidal Fitting

100 g, 75%, 920 cc



# IV. Sigmoidal Fitting

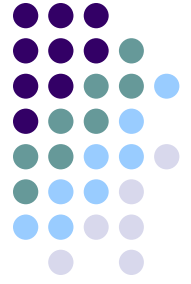
100 g, 75%, 920 cc



**f1 = 982**

**f3 = 5.93**

**f4 = 2.04**



# IV. Master Fit for $T = F(m, V, P, t)$

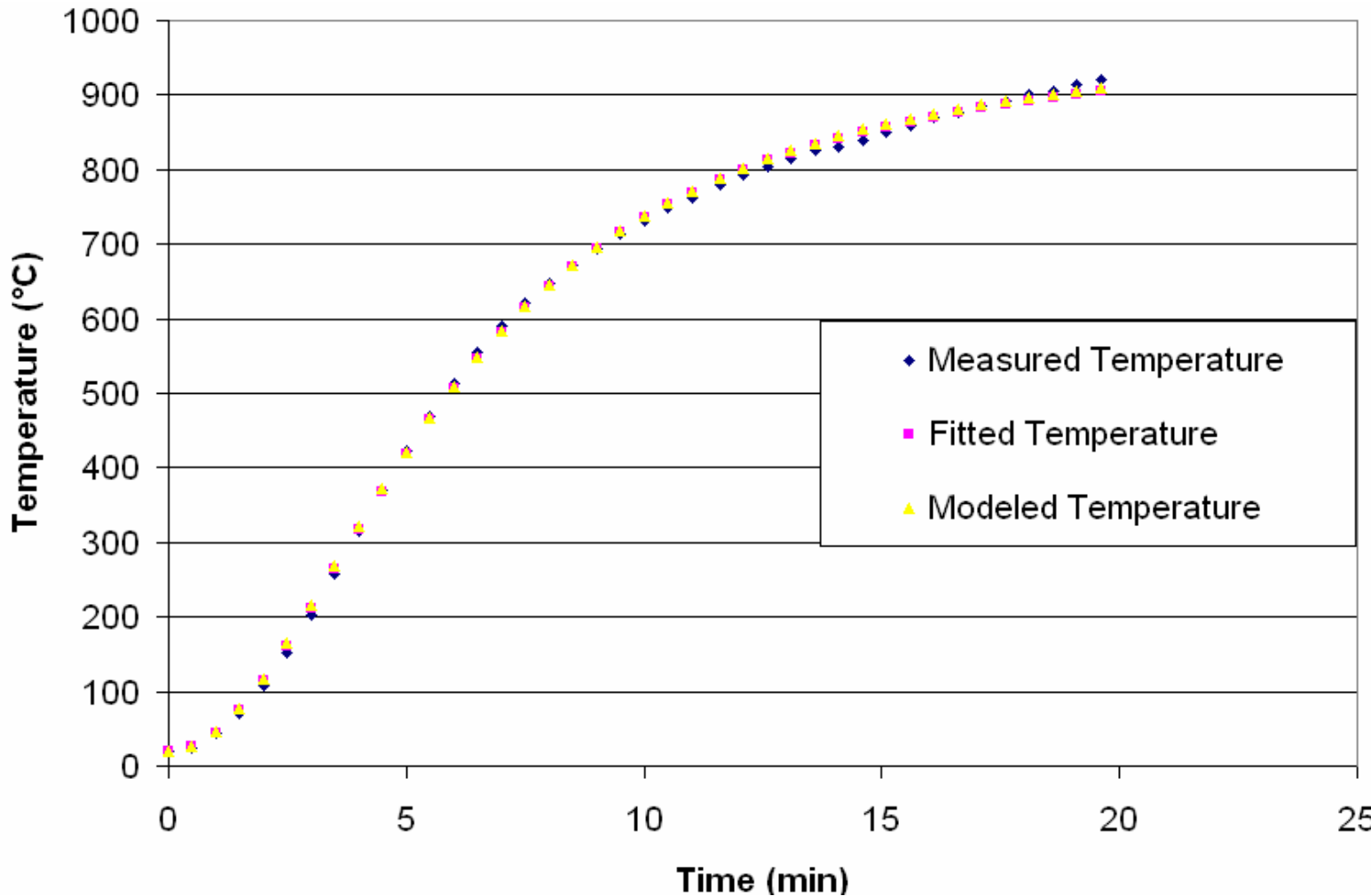
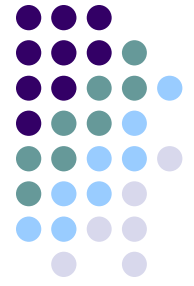
Coded Variables	<b>m</b>	<b>P</b>	<b>V</b>
	-1	-1	-1
	0	0	0
	1	1	1.4

$$F(t) = c1 + \frac{(c2 - c1)}{\left(1 + \left(\frac{t}{c3}\right)^{c4}\right)}$$

$$T = (1171 + 84m + 111p - 129v + 21mp) + \frac{(T_o - 1171 + 84m + 111p - 129v + 21mp)}{\left(1 + \left(\frac{t}{5.92 + 1.47m - 1.3p - v + 0.32pv + 0.73v^2}\right)^{2.14 - 0.091v + 0.045v^2m - 0.085m^2}\right)}$$

# IV. Sigmoidal Fitting

100 g, 75%, 920 cc



**f1 = 982**

**f3 = 5.93**

**f4 = 2.04**



**Linear regression**



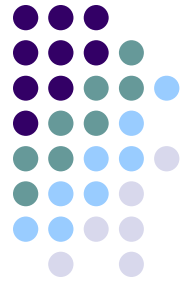
**m1 = 991**

**m3 = 5.96**

**m4 = 2.01**



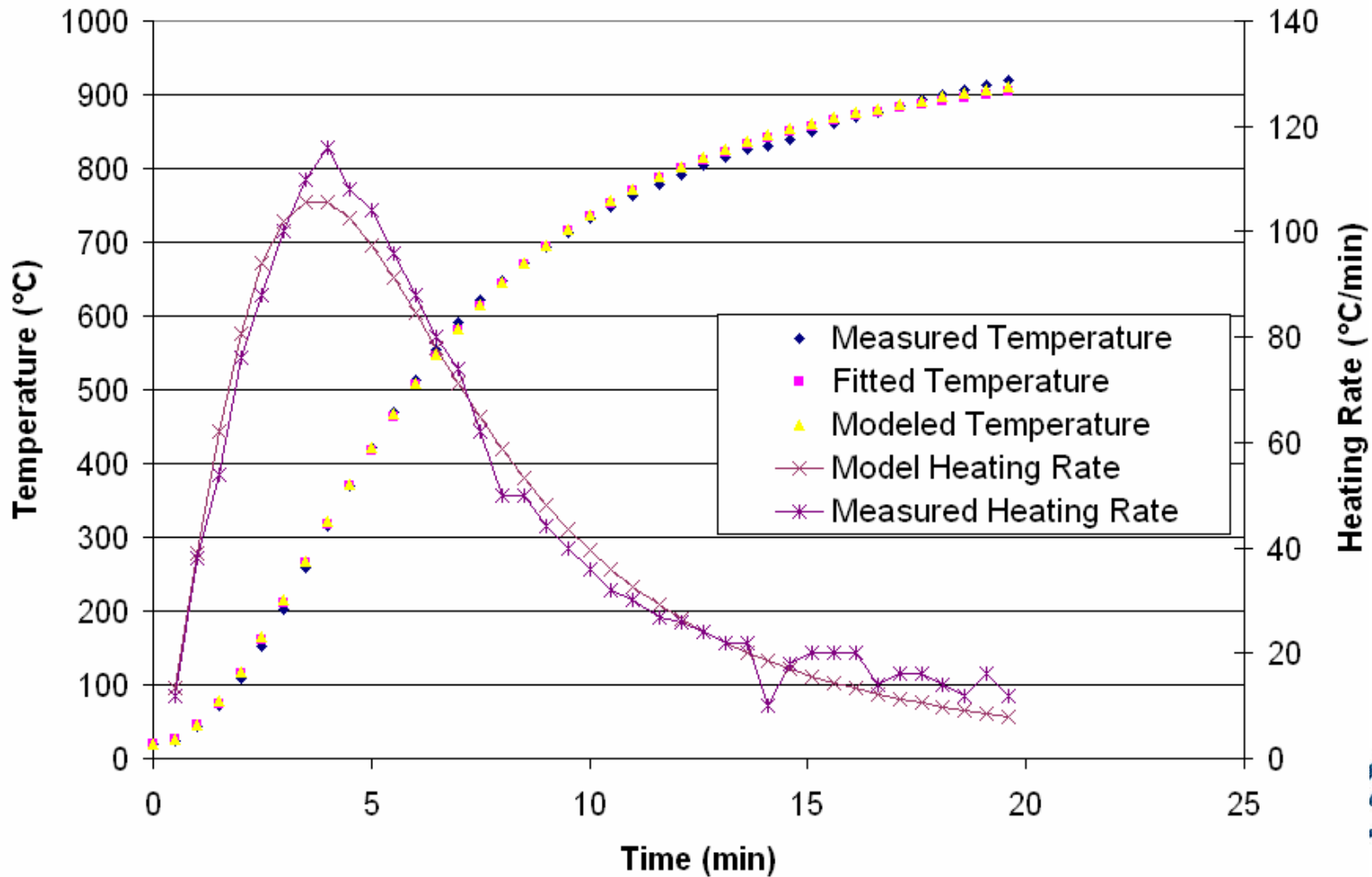
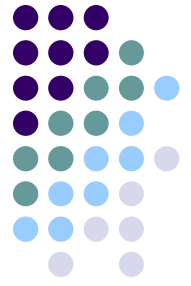
## IV. Master Fit of Heating Rate



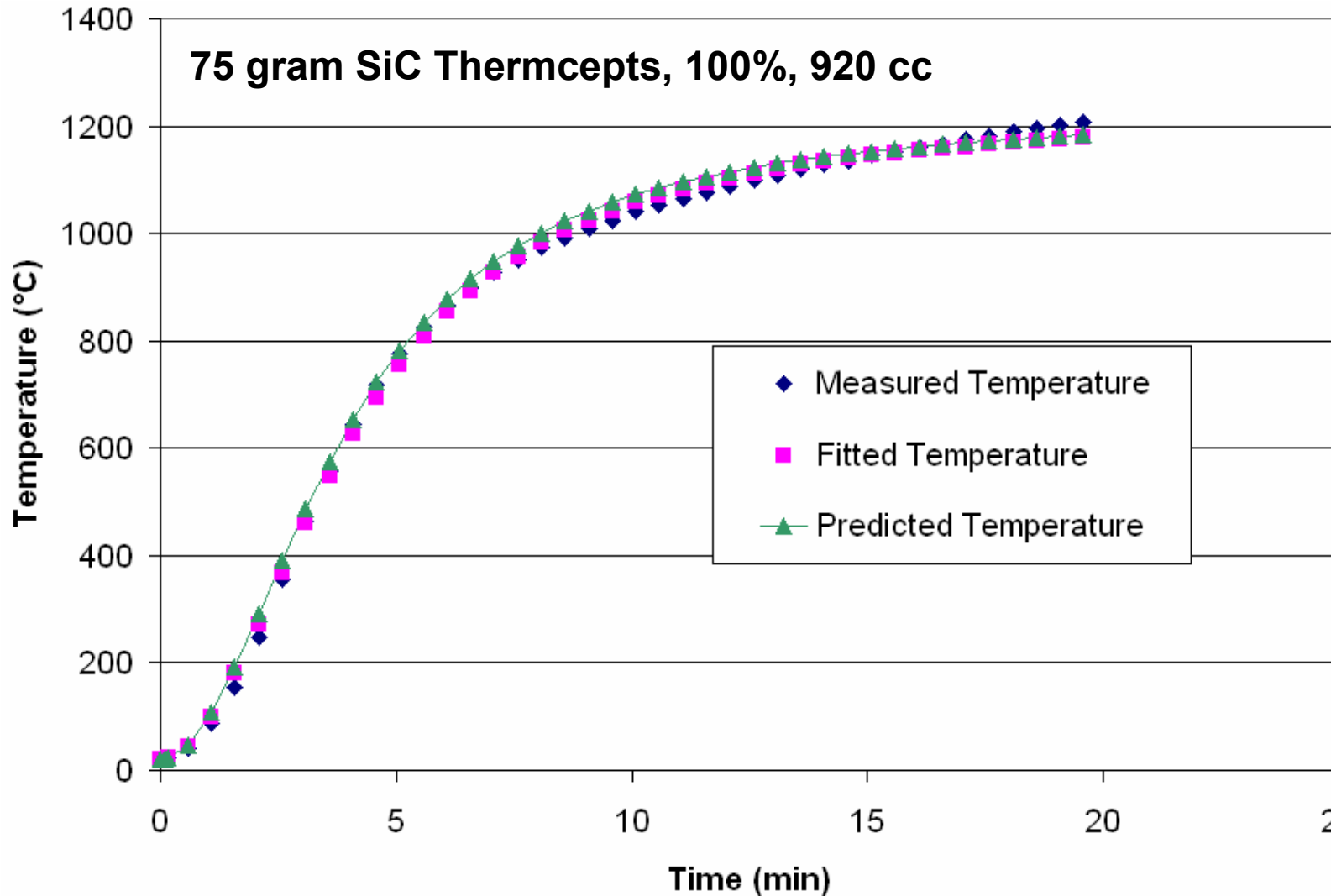
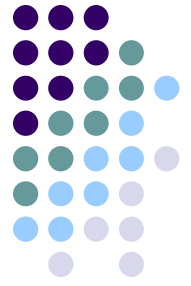
$$\frac{\partial T}{dt} = \frac{c4(c2 - c1)t^{c4-1}}{c3^{c4} \left( 1 + \left( \frac{t}{c3} \right)^{c4} \right)^2}$$

# IV. Sigmoidal Fitting

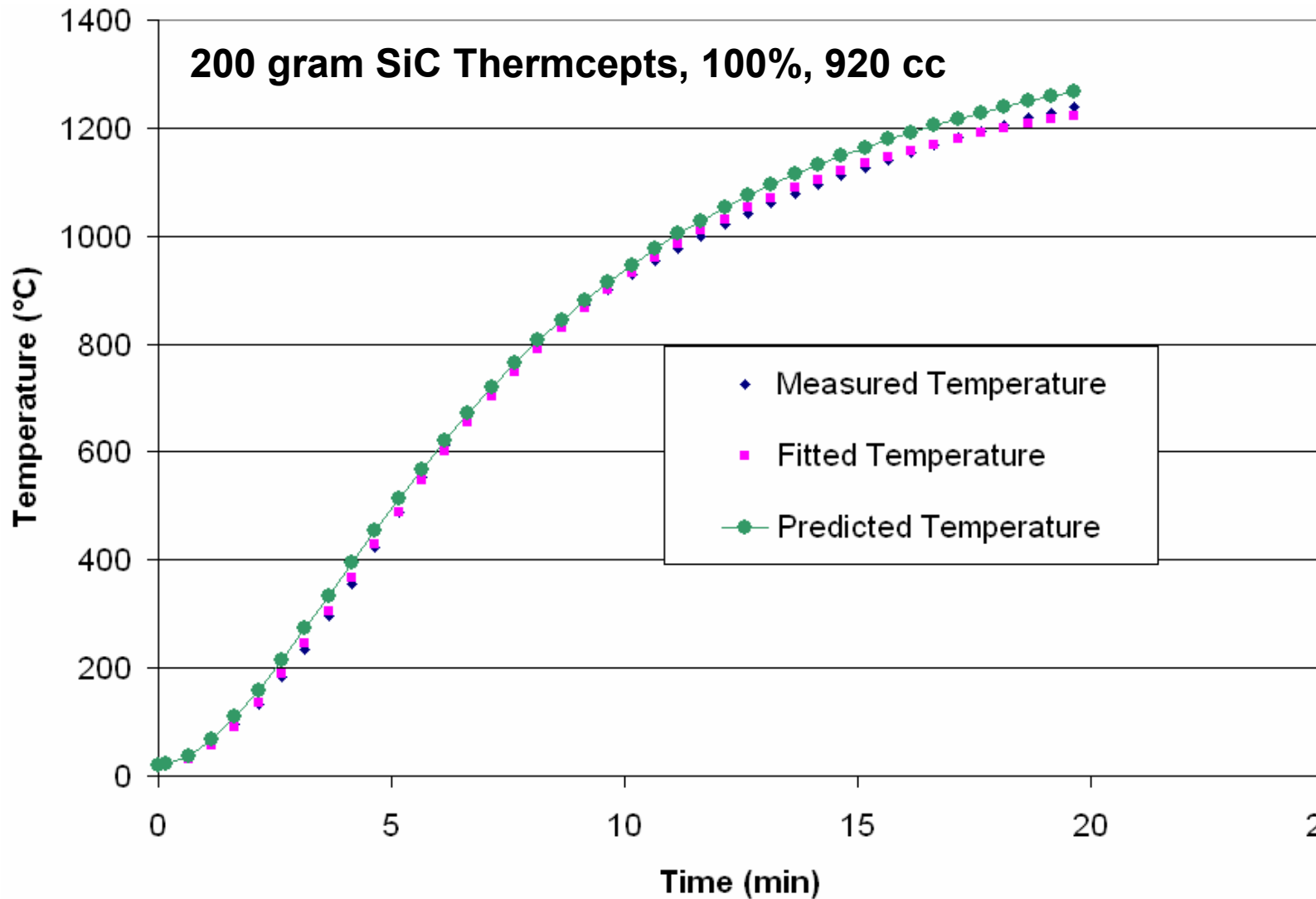
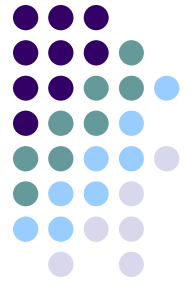
100 g, 75%, 920 cc

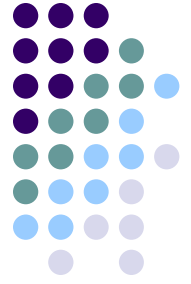


# V. Testing the Model: Interpolation of Master Fit



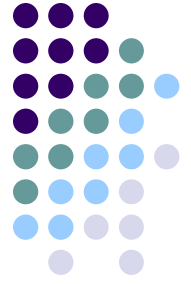
# V. Testing the Model: Extrapolation of Master Fit





## VI. Conclusions

- Empirical models can be applied to standardized high temperature susceptor assisted microwave heating
- Fit of model indicates reproducibility of susceptor assisted heating data
- Model can be used to predict heating profiles
- Method for modeling other susceptor systems
- Coefficients provide links to physical models



# Acknowledgements

- Dr. Timothy Keith
- John Byrnes

## Questions?